Feeling Paramagnetic Micro-Particles Trapped Inside Gas Bubbles: A Tele-Manipulation Study

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Abstract—Surface tension forces, pressure forces, and drag forces arise once a micro-particle comes into contact with a gas bubble or a biological cell in diverse physical and biomedical applications such as targeted therapy, sorting, and characterization of cancer cells. We experimentally demonstrate that these forces can be estimated, scaled-up to the sensory range of a human operator, and sensed during a transparent bilateral tele-manipulation using an electromagnetic system and a haptic device. We find good agreement between the estimated interaction forces and the measured forces using a calibrated microforce sensing probe. The maximum interaction force between a trapped paramagnetic micro-particle and an oxygen bubble is estimated to be $4 \mu N$. The estimated interaction force is scaled-up and used in the design of a tele-manipulation system (haptic device and an electromagnetic system) that enables motion control of the bubble in a two-dimensional space, while sensing the interaction forces with the bubble. We demonstrate experimentally that the operator senses maximum interaction force (surface tension, pressure, and drag forces) with the same order of magnitude as the calculated theoretical forces. The estimation of interaction forces at this scale provides broad possibilities in targeted therapy and characterization of cancer cells.

I. INTRODUCTION

Interaction forces arise during applications such as manipulation of biological cells [1], molecules [2], and high-precision particle separation [3]. Accurate estimation or measurement of these forces to avoid damage is essential for many biological [4], [5] (penetration of cancer cells using nano-motors in targeted drug delivery), physical [6] (study of the particle-to-particle interactions, van der Waals force, and thermophoretic effects), and chemical [7], [8], [9] (catalytic-based micro-motors and nano-particle accumulation) studies. The first controlled manipulation of molecular samples has been achieved by Guthold et al. with a nano-manipulator [10]. This nano-manipulator has allowed for the visualization and manipulation of molecular samples using atomic-force microscope (AFM). In biomedical applications, the AFM probes could easily contaminate and damage the walls of the samples during scanning or manipulation. Bukusoglu et al. [11] have overcome this problem by achieving haptic manipulation of micro-spheres using optical tweezers and artificial force fields. The micro-manipulation systems become less flexible and difficult to automate due to the scale of the micro- and nano-manipulation, and the predominant adhesive forces (over inertial and gravitational forces). This problem can be overcome by adapting the current tele-manipulation systems [12], [13], [14], [15] to include electromagnetic coils at the slave-side (Fig. 1(a)) to allow for the wireless non-contact micro-manipulation [16], instead of the contact manipulation used by the AFM probes, for instance. We present a theoretical analysis and experimental tele-manipulation of trapped paramagnetic micro-particles inside gas bubbles. First, we analyze the interaction forces of a trapped micro-particle in a gas bubble (a) The manipulation is achieved under the influence of the magnetic field gradients exerted on the magnetic dipole of the micro-particle. The controlled gradients are generated using an electromagnetic system (upper-left corner). The interaction forces between the trapped micro-particle and the bubble (black arrow) are measured and scaled-up to the sensory range of the operator (bottom-left inset). The operator moves the micro-particles towards the small blue circle (blue arrow) and feels the scaled drag, pressure, and surface tension forces on the haptic device (bottom-left corner). (b) A potential application of the electromagnetic-based tele-manipulation is targeting and characterization of cancer cells using cluster of nano-particles [5]. The dashed white and black arrows indicate cluster of nano-particles and a cancer cell (U-373 MG human astrocytoma cells).

Fig. 1. Electromagnetic-based tele-manipulation of a gas bubble (700 $\mu$m in diameter) using a trapped paramagnetic micro-particle (100 $\mu$m in diameter).
forces between the micro-particles and the bubble using a calibrated force observer (we expand on the work of [18], [19], [20] which has not verified the accuracy of the estimated forces). This calibration is done using a microforce sensing probe that is incorporated to measure the interaction forces on the micro-particle. The estimation of the interaction forces at this scale and comparison with measured forces is not documented in prior literature. Second, the estimated forces are scaled-up to the sensory range of the operator [21] and used to manipulate gas bubbles in two-dimensional (2D) space under the influence of the controlled magnetic field gradient and using microscopic feedback. The tele-manipulation system consists of a haptic device (pantograph mechanism) and an electromagnetic system with 4 orthogonal electromagnetic coils (Fig. 1(a)). The haptic device allows the operator to provide reference trajectories to the controlled bubble. The electromagnetic configuration surrounds a water reservoir that contains the micro-particles and the gas bubbles (gas bubbles are used instead of biological cell (Fig. 1(b)) to verify the accuracy of the force observer), and their positions are determined using a microscopic system and a high speed camera. The remainder of this paper is organized as follows: Section II provides descriptions pertaining to the interactions between a paramagnetic micro-particle and a gas bubble under the influence of magnetic field and hydrodynamic forces. Section III presents a tele-manipulation control system based on force estimation. Finally, Section IV provides conclusions and directions of future work.

II. MODELING OF THE INTERACTION BETWEEN PARAMAGNETIC MICRO-PARTICLE AND GAS BUBBLE

The interactions between the micro-particle and the gas bubble can occur when the micro-particle is outside or trapped inside the bubble, as shown in Fig. 2. The micro-particle is trapped inside a gas bubble manually by ejecting air bubbles gradually using a syringe needle inside a water reservoir that contains the micro-particles. In low-Reynolds-regime fluids, the balance of the force components along the radial direction is given by [22]

\[ \mathbf{F}_m(P) + \mathbf{F}_{sp} + \mathbf{F}_p + \mathbf{F}_d(P) = m \ddot{P} = 0, \]  

where \( \mathbf{F}_m(P) \in \mathbb{R}^{2x1} \) and \( \mathbf{F}_{sp} \in \mathbb{R}^{2x1} \) are the magnetic force (at point \( P \in \mathbb{R}^{2x1} \)) and the surface tension force exerted on the micro-particle, respectively. Further, \( \mathbf{F}_p \in \mathbb{R}^{2x1} \) and \( \mathbf{F}_d \in \mathbb{R}^{2x1} \) are the pressure force and the drag force on the micro-particle with mass \( m \), respectively. The inertial term \( (m \ddot{P} \in \mathbb{R}^{2x1}) \) is included in (1) based on the Reynolds number of the micro-particle. For a cluster of less than 4 micro-particles, Reynolds number is calculated to be 0.024 (at average speed of 120 \( \mu \)m/s) and the inertial terms can be neglected in (1). For cluster of 8 micro-particles, Reynolds number is calculated to be 0.19 (at average speed of 494 \( \mu \)m/s). The micro-particles are paramagnetic and consist of iron-oxide in a polyactic acid matrix (PLAParticles-M-redFplain from Micromod Partikeltechnologie GmbH, Rostock-Warnemünde, Germany). The magnetic force is controlled using the following external magnetic field gradient [23]:

\[ \mathbf{F}_m(P) = \nabla (m \cdot \mathbf{B}(P)) = \nabla (m \cdot \mathbf{B}(P) I), \]  

In (2), \( m \in \mathbb{R}^{2x1} \) and \( \mathbf{B}(P) \in \mathbb{R}^{2x1} \) are the magnetic dipole moment of the micro-particle and the external magnetic field, respectively. Further, \( \mathbf{B}(P) \in \mathbb{R}^{2x1} \) and \( I \in \mathbb{R}^{4x1} \) are the magnetic field-current map [24] and the input current to the electromagnetic coils, respectively. The pressure force exerted on the micro-particles at the water-gas interface is given by [25]

\[ \| \mathbf{F}_p \| = \frac{2\pi \gamma}{R_b} \left( R_p \sin(\theta) \right)^2, \]  

where \( \gamma \) is the surface tension. Further, \( R_p \) and \( R_b \) are the radius of the micro-particle and the radius of the bubble, respectively, and \( \theta \) is demonstrated in Fig. 2. The pressure force \( \mathbf{F}_p \) is due to the following pressure difference between the gas \( (P_g) \) and the water \( (P_w) \):

\[ P_w - P_g = \frac{2\gamma}{R_b} \]  

The surface tension force \( \mathbf{F}_{sp} \) is given by:

\[ \| \mathbf{F}_{sp} \| = 2\pi \gamma R_p \sin \theta. \]  

Further, the surface tension force on the micro-particle \( \mathbf{F}_{sp} \) is

\[ \mathbf{F}_{sp} = \mathbf{F}_s \sin(|\theta - \gamma|). \]  

In (1), the drag force on the trapped micro-particle inside the bubble is calculated using Stokes’ law:

\[ \mathbf{F}_d(P) = 6\pi \eta R_b \dot{P}, \]
where $\eta$ is the dynamic viscosity and $\mathbf{\hat{P}}$ is the velocity vector of the bubble (we assume that the trapped micro-particle and the bubble have similar velocity). The input current $\mathbf{I}$ to the electromagnetic coils and the measured velocity vector of the micro-particle ($\mathbf{\hat{P}}$) are used to estimate the last three forces in (1). The following force observer is used to estimate these forces [18], [26]:

$$\mathbf{\hat{F}}_{\text{par}}(\mathbf{\hat{P}}) = \frac{g}{s + g} \left( \nabla (m \cdot \mathbf{\hat{B}}(\mathbf{P}) \mathbf{I}) + gm \mathbf{\hat{P}} \right) - gm \mathbf{\hat{P}}, \quad (8)$$

where $\mathbf{\hat{F}}_{\text{par}} \in \mathbb{R}^{2 \times 1}$ is the estimated drag, pressure, and surface tension forces on the micro-particle. Further, $g > 0$ is the positive-gain of the force observer. Furthermore, $s$ is the Laplace operator. Experiments are done within a square workspace. The electromagnetic coils provide an average magnetic field ($|\mathbf{B}(\mathbf{P})|$) and field gradient ($\frac{\partial \mathbf{B}(\mathbf{P})}{\partial \mathbf{P}}$) within this workspace. The haptic device is a pantograph mechanism that consists of 2 active links of length ($l_1$) and 2 passive links of length ($l_2$). Two DC motors (2322 980, Maxon Motor, Sachseln, Switzerland) are used to control the active links. We calculate the net drag, surface tension, and pressure forces on the micro-particle and a gas bubble with average diameters of $R_p$ and $R_b$, respectively. With the knowledge of the water dynamic viscosity ($\eta$) and surface tension ($\gamma$) and using the parameters in table 1, the maximum net interaction force (upper-bound) on the micro-particle is calculated to be $8 \times 10^{-7}$ N, at an average speed of $300 \ \mu m.s^{-1}$, for the trapped micro-particle in the bubble. In order to verify the accuracy of the force observer (8), we measure the interaction force on a cluster of 3 micro-particles with the tip of the micro-force sensing probe (FT-S100 Microforce Sensing Probe, FemtoTools AG, Buchs, Switzerland). The tip of the micro-force sensing probe is moved gradually to the water-gas interface using a three-dimensional motion stage. The magnetic field gradient (using (2)) provides a pulling force to the micro-particles towards the tip of the probe, as shown in Fig. 4. We observe that the measured force increases gradually as the micro-particles approaches the tip, and a pick force of 0.7 $\mu$N is measured, at time, $t=6$ seconds, upon the contact between the micro-particles and the tip of the sensing probe. Fig. 5 provides a representative comparison between the measured interaction force and the estimated force using (8). This estimation can be controlled by changing the observer gain ($g$). Increasing this gain provides faster convergence and undesirable measurement noise. Therefore, we set the force observer gain to 10 rad.s$^{-1}$ throughout our experiments, and use (8) in the design of the bilateral tele-manipulation control.

### III. Design of Bilateral Control System

As shown in Fig. 3. The red and blue lines represent the measured and estimated interaction forces, respectively (Fig. 4). At time, $t = 1.5$ seconds, the micro-particles touches the tip of the sensor and a peak force of -0.72 $\mu$N is measured (compression force). The estimated interaction force (red line) indicates that the observer can be used instead of the force sensor. The fluctuation in the estimated force can be eliminated by decreasing the gain of the force observer ($g$). However, it is important to consider the trade-off between noise attenuation and convergence speed of the observer [20]. We also estimate the interaction forces between the haptic device and the operator to design the bilateral tele-manipulation system (bottom-left inset in Fig. 1(a)). The interaction force at the haptic device is given by [26]:

$$\mathbf{\hat{F}}_{\text{hap}} = \frac{g}{s + g} \left( \mathbf{K}_t + g \mathbf{M}_m \dot{\mathbf{x}} \right) - g \mathbf{M}_m \dot{\mathbf{x}}, \quad (9)$$

where $\mathbf{\hat{F}}_{\text{hap}} \in \mathbb{R}^{2 \times 1}$ is the interaction force between the operator and the haptic device. Further, $\mathbf{K}_t \in \mathbb{R}^{2 \times 2}$ and $\mathbf{M}_m \in \mathbb{R}^{2 \times 2}$ are the matrix of the torque constants of the haptic device and its inertia matrix, respectively. Furthermore, $\dot{\mathbf{x}} \in \mathbb{R}^{2 \times 1}$ is the velocity vector of the of the interaction point between the operator and the haptic device. The position

<table>
<thead>
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<th>Parameter</th>
<th>Value</th>
<th>Parameter</th>
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<td>$</td>
<td>\mathbf{B}(\mathbf{P})</td>
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<td>$l_1$ [mm]</td>
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<td>$l_2$ [mm]</td>
<td>153</td>
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TABLE I. CHARACTERISTICS OF OUR BILATERAL CONTROL SYSTEM. THE SYSTEM CONSISTS OF A HAPTIC DEVICE (MASTER) AS THE PANTOGRAPH MECHANISM AND A MAGNETIC SYSTEM (SLAVE) COMPOSED OF AN ORTHOGONAL ARRAY OF FOUR ELECTROMAGNETS, WITH A WORKSPACE AREA OF 1.3MM X 1.3MM.
\((\mathbf{e}_p \in \mathbb{R}^{2 \times 1})\) and force \((\mathbf{e}_f \in \mathbb{R}^{2 \times 1})\) tracking errors of the tele-
manipulation are calculated using

\[
\mathbf{e}_p = \mathbf{x} - \alpha \mathbf{P} \quad \text{and} \quad \mathbf{e}_f = \mathbf{F}_{\text{hap}} + \beta \mathbf{F}_{\text{par}},
\]

where \(\alpha > 0\) and \(\beta > 0\) are position and force scaling coefficients, and \(\mathbf{x} \in \mathbb{R}^{2 \times 1}\) is the position of the interaction point between the haptic device and the operator. Using (10), we define a generalized position tracking error \((\sigma \in \mathbb{R}^{2 \times 1})\) as follows:

\[
\sigma = \mathbf{e}_p + \epsilon \mathbf{e}_p.
\]

In (11), \(\epsilon\) is a positive control gain, and finally we devise the following variables to achieve asymptotic convergence:

\[
\Gamma_p = -k_p \sigma \quad \text{and} \quad \Lambda_f = -k_I D_h^{-1} \mathbf{e}_f,
\]

where \(\Gamma_p \in \mathbb{R}^{2 \times 1}\) and \(\Lambda_f \in \mathbb{R}^{2 \times 1}\) are the desired accelerations in the position and force loops, respectively. The tele-
manipulation gains \((k_p > 0)\) and \((k_I > 0)\) are positive, and \(D_h\) is the damping coefficient of the operator hand. Finally, the control input to the haptic device \((\mathbf{F})\) and the input magnetic force \((\mathbf{F}_m)\) are calculated using:

\[
\mathbf{F} = \frac{\mathbf{M}_m}{\alpha + \beta} (\alpha \Lambda_f + \beta \Gamma_p) \quad \text{and} \quad \mathbf{F}_m = \frac{1}{\alpha + \beta} (\Lambda_f + \Gamma_p).
\]

We substitute (13) in the equation of motion of the haptic device

\[
\mathbf{M}_m(q) \ddot{\mathbf{x}} + \mathbf{c}_m(q, \dot{q}) = \mathbf{F} - \mathbf{f}_o,
\]

where \(\mathbf{c}_m(q, \dot{q})\) is the Coriolis damping of the haptic device and \(\mathbf{f}_o\) is the interaction force between the haptic device and

the operator. This substitution yields the following acceleration:

\[
\ddot{x} = \frac{1}{\alpha + \beta} (-\alpha k_I D_h^{-1} \mathbf{e}_f - \beta k_p \sigma).
\]

Similarly, substituting (13) in (1) yields

\[
\ddot{\mathbf{P}} = \frac{1}{\alpha + \beta} (-\alpha k_I D_h^{-1} \mathbf{e}_f + k_p \sigma).
\]

Finally, the position tracking error of the bilateral control system is calculated using (11), (12), (15), and (16), as follows:

\[
\ddot{\mathbf{e}}_p = \ddot{x} - \alpha \ddot{\mathbf{P}} = -k_p \epsilon \mathbf{e}_p - k_p \epsilon \mathbf{e}_p.
\]

Therefore, the error dynamics between the micro-particle and haptic device is governed by

\[
\ddot{\mathbf{e}}_p + k_p \epsilon \mathbf{e}_p + k_p \epsilon \mathbf{e}_p = 0.
\]

The control gains \(k_p\) and \(\epsilon\) have to achieve stable roots of the characteristic polynomial of (18). The position of the end-
effector of the master-robot is determined via the kinematic equations of the haptic device using its active angles. The position of the micro-particle is determined using a feature tracking algorithm and a microscopic vision system.

Implementation of the control laws (13) is shown in Fig. 6. Force observers (8) and (9) are designed at the haptic device and the electromagnetic configuration, respectively. The operator moves the haptic device and provides reference trajectory (indicated using the small blue circle) in 2D space, as shown in Fig. 6. This reference trajectory is scaled-down \((\alpha=2285)\) to micro-scale to control the motion of the micro-particle based on the motion of the operator. The estimated interaction force
Fig. 7. Estimated forces of the micro-particle and the haptic device (task space forces) during a tele-manipulation trial. The red and blue lines indicate the estimated scaled force of the haptic device and the estimated force of the micro-particles, respectively.

IV. CONCLUSIONS AND FUTURE WORK

In conclusion, we present an experimental study for the tele-manipulation of a gas bubble under the influence of the controlled magnetic fields exerted on a trapped micro-particle. The surface tension forces, pressure forces, and drag forces on the trapped micro-particles are estimated, scaled-up to our sensory range, and sensed by the operator. The estimated force is verified using measurement taken by a calibrated microforce sensing probe, during the interaction of micro-particles with the sensor tip. We also compare the calculated forces and show that they have the same order of magnitude as the scaled sensed force by the operator. The demonstration of the tele-manipulation and scaled sensing of the interaction force with gas bubbles is an important step towards safe manipulation and handling of biological cells in targeted therapy and biomedical applications.

As part of future studies, targeted therapy using tele-manipulation and penetration will be achieved in vitro. In addition, the tele-manipulation will be done in three-dimensional space [27]. Furthermore, sorting of cells will be done using our tele-manipulation system with interaction force feedback during the manipulation process to achieve force-controlled manipulation to avoid cell contamination or permanent damage to the cell membrane during contact manipulation.

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REFERENCES

(a) Tele-Manipulation trials

(b) Force error of each trial

Fig. 8. Representative tele-manipulation trials of gas-bubbles using paramagnetic micro-particles. (a) Four tele-manipulation trials of paramagnetic micro-particles, and the interaction forces on the micro-particles (blue line) and haptic device (red line) are measured. These trials are done to allow the operator to sense forces at the micro-scale. (b) The median force error is approximately 1.86 μN.


